# 2DM10 Studeerwijzer 2010–2011

# Algemene Informatie

Assistenten begeleide zelfstudie 2DM10 2010-2011:

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Zaalindeling begeleide zelfstudie 2DM10 2010-2011:

- HG 6.96 (zaalcapaciteit ca. 36): Rik Kaasschieter & Bas Willems
- HG 6.09 (zaalcapaciteit ca. 48): Adrian Muntean & Arris Tijsseling & Rozemarijn Weijers

Verantwoordelijk docent 2DM10 2010-2011:

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Boek: Calculus: A Complete Course, Robert Adams & Christopher Essex,  $7^{\rm de}$ editie © 2010

## Studeerwijzer

- W = werkcollege, C = college, BZ = begeleide zelfstudie
- BZ exercises requiring a calculator or Matlab may be ignored
- this not necessarily complete information is provided for your convenience, no rights can be inferred from it

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- W 9-11-2010: C-numbers, Appendix I
- C 10-11-2010: C-functions, Appendix II
  - $\mathbb{C}$ -functions in general and graphical representation
  - $\mathbb{C}$ -polynomials
- BZ 11–11–2010: odd exercises Appendix I

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- W 16–11–2010: C-functions, Appendix II:
  - algebraic manipulation of C-polynomials
  - fundamental theorem of algebra (without proof)
  - definition and graphical representation  $\mathbb{C}$ -exponential function
- C 17–11–2010: differentiation, chapter 2 (refreshment of 2DM00: "basis wiskunde")
  - standard functions and their derivatives, pp. 101–124
  - general differentiation rules, pp. 107–118
  - mathematical induction ("volledige inductie"), p. 109
- BZ 18-11-2010: odd exercises 2.3, p. 114 & 2.4, p. 119 & 2.5, pp. 124-125

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#### • W 23–11–2010:

- mean value theorem and corollaries, pp. 136–142

# • C 24–11–2010:

- linear approximations, pp. 266–271
- Taylor polynomials, pp. 271–279

• BZ 25-11-2010: odd exercises 2.8, p. 142 & 4.9, p. 271 & 4.10, pp. 279-280

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#### • W 30–11–2010:

- proof of Taylor's theorem, pp. 271–275
- big- $\mathcal{O}$  notation, pp. 276–279
- Taylor formulas for standard functions, p. 277
- $\Sigma$ -notation, pp. 288–292
- partitions, upper and lower Riemann sums, definite integral, pp. 299–302

## • C 1–12–2010:

- general Riemann sums, pp. 303–304
- properties of definite integral, pp. 305–307
- mean value theorem for definite integral, pp. 308–309
- fundamental theorem of calculus, pp. 311–315

# • BZ 2–12–2010:

- odd exercises Appendix II, p. A-19 (except 19, 21)
- odd exercises 4.10, pp. 279–280
- exercises 5.1: 11, 13, 33, 35–38 (prove formulas 35–38 via mathematical induction)
- odd exercises 5.5 up to 45

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## • W 7–12–2010:

- method of substitution, pp. 316–322
- C 8–12–2010:
  - integration by parts, pp. 331-336

# • BZ 9–12–2010:

- $\ {\rm exercises} \ 5.6, \ {\rm pp.} \ 323 324 {\rm :} \ 1, \ 3, \ 5, \ 7, \ 9, \ 11, \ 13, \ 15, \ 17, \ 19, \ 21, \ 23, \ 25, \ 27, \ 33, \ 41, \ 43$ 
  - \* hint 11: rewrite in terms of  $\cosh x$  and  $\sinh x$  and recall  $\cosh' x = \sinh x$ ,  $\sinh' x = \cosh x$
  - \* hint 19:  $y = \ln \cos x$  (it is assumed that x is such that  $\cos x > 0$ )
  - \* hint 21:  $x^2 + 6x + 13 = 4((\frac{1}{2}x + \frac{3}{2})^2 + 1)$
- exercises 6.1, pp. 336-337: 1, 3, 5, 7, 13, 19, 21, 37
  - \* hint 7:  $\arctan x = 1 \cdot \arctan x$  (b.t.w.  $\tan^{-1} = \arctan(x)$

- \* hint 13: perform integration by parts twice
- \* hint 19:  $\cos(\ln x) = 1 \cdot \cos(\ln x)$  (it is assumed that x > 0)
- \* hint 21: substitution of variables and integration by parts are both applicable: try!

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#### • W 14–12–2010:

- standard limits:  $\lim_{x \to \infty} x^n e^{-x} = \lim_{x \to \pm \infty} x^n e^{-x^2} = \lim_{x \to 0} x^{n+1} \ln |x| = 0 \text{ for } n \ge 0$
- integral of a rational function, pp. 337–345
- classification of ordinary differential equations (ODEs):
  - $* n^{\text{th}}$  order linear (in)homogeneous ODEs with (non)constant coefficients
  - \* 1<sup>st</sup> order (non)linear separable ODEs

# • C 15–12–2010:

- section 2.10, pp. 147–152
- section 3.7, pp. 203–209 (especially cases I, II, and III)
- section 7.9, pp. 445–453 (separable ODEs only)
- section 17.1, pp. 938–940 (especially Theorem 1 and Theorem 2)

## • BZ 16–12–2010:

- exercises 2.10, p. 153: 27-45 (odd numbered only), 44
- exercises 3.7, pp. 209–210: 13, 14, 15, 19, 21
- exercises 7.9, pp. 452-453: 1, 3, 5, 7, 9, 13, 15, 17

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## • W 4–1–2011:

- section 17.5, pp. 957–961 (2<sup>nd</sup> order only except Euler equations)
- section 17.6, pp. 961–967 (only the method of "educated guessing" or "undetermined coefficients" for constructing particular solutions)
- C 5–2–2011:
  - section 7.9, pp. 445–453 (first order linear ODEs only)
  - section 17.5, pp. 957–961 (higher order only except Euler equations)
  - typical examination examples
- BZ 6–1–2011:
  - exercises 17.1, pp. 940–941: 1, 3, 5, 7, 9, 11, 17

- exercises 17.5, p. 961: 1, 3, 5
- exercises 17.6, pp. 967-968: 1, 3, 5, 7, 9
  - \* hint 1: stipulate a particular solution of the form  $y_{\rm p}(x) = ax + b$
  - \* hint 3: stipulate a particular solution of the form  $y_{\rm p}(x) = ae^{bx}$
  - \* hint 5: stipulate a particular solution of the form  $y_{\rm p}(x) = ax^2 + bx + c$
  - \* hint 7: stipulate a particular solution of the form  $y_p(x) = (ax + b)e^{cx}$
  - \* hint 9: stipulate a particular solution of the form  $y_p(x) = (a \sin x + b \cos x)e^{cx}$

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## • Exams January 19 & April 13, 2011:

- all theory and exercises outlined above, except subjects in *italics*
- all theory and examples covered in the oral lectures
- those parts of "Calculus: A Complete Course" relating to the above
- only pen and paper are allowed, i.e. no calculator, laptop, notes or other material
- it is strongly recommended to practice with old exams in addition